XIII. Extract of a Letter from the Right Honourable Philip Earl Stanhope, F. R. S. to Mr. James Clow, Professor of Philosophy in the University of Glasgow. Dated Chevening, February 16, 1777.

Read June 10, 1780.

HAVE lately made some curious observations concerning the roots of adsected equations, part of which have occurred to Messieurs daniel bernoulli, euler, de la grange, lambert, and others; but some of them, I believe, are quite new. I will give you one instance of a quadratic equation, as the simplest.

Let the quadratic equation 11xx - 15x + 5 = 0, be proposed. I say then, that if two recurring series be formed from the fractions $\frac{1+2z}{1-z-zz}$, $\frac{2+3z}{1-z-zz}$, which have a common denominator, and each series of co-efficients, continued both ways (that is, as well before, as after the first term) the fractions formed by dividing each term of the first series by the corresponding term of the second feries, viz.

&c. $\frac{-11}{-14}$, $\frac{+7}{+9}$, $\frac{-4}{-5}$, $\frac{+3}{+4}$, $\frac{-1}{-1}$, $\frac{-3}{-4}$, $\frac{2}{3}$, $\frac{1}{2}$, $\frac{1}{5}$, $\frac{4}{7}$, $\frac{7}{12}$, $\frac{11}{19}$, $\frac{18}{31}$, $\frac{29}{50}$ &c. will converge in the simplest manner possible; those before the bar, in a retrograde order to the greater root $\frac{15+\sqrt{5}}{22}$; and those after the bar, in a direct order to the simallest root $\frac{15-\sqrt{5}}{22}$; where it is to

C c 2 be

be observed, that the greater root is affirmative, notwithstanding the sign – being prefixed to some of the terms, because in each fraction the numerator and the denominator are affected by the same sign, whether + or -.

The chief improvement I have made confifts in approximating to two roots at once, by one and the same series, continued backwards as well as forwards. I have not time to enlarge upon this subject at present; but the little I have said will be a specimen of the method to be used in higher equations.

